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INCOME RISK OF EU COAL-FIRED POWER PLANTS AFTER KYOTO

by

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Income risk of EU coal-fired power plants after Kyoto

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Abstract

Coal-fired power plants may enjoy a significant advantage relative to gas plants in terms of cheaper fuel cost. Still, this advantage may erode or even turn into disadvantage depending on CO2 emission allowance price. This price will presumably rise in both the Kyoto Protocol commitment period (2008-2012) and the first post-Kyoto years. Thus, in a carbonconstrained environment, coal plants face financial risks arising in their profit margins, which in turn hinge on their so-called 'clean dark spread'. These risks are further reinforced when the price of the output electricity is determined by natural gas-fired plants' marginal costs, which differ from coal plants' costs.

We aim to assess the risks in coal plants' margins. We adopt parameter values estimated from empirical data. These in turn are derived from natural gas and electricity markets alongside the EU ETS market where emission allowances are traded. Monte Carlo simulation allows to compute the expected value and risk profile of coal-based electricity generation. We focus on the clean dark spread in both time periods under different future scenarios in the allowance market. Specifically, bottom 5% and 10% percentiles are derived. According to our results, certain future paths of the allowance price may impose significant risks on the clean dark spread obtained by coal plants.

Keywords: Clean dark spread, clean spark spread, EU Emissions Trading Scheme, Monte Carlo.

JEL Codes: C6; E2; D8, G3.

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1 Introduction

One of the main and most obvious consequences of electricity market liberalization is the fact that now utilities provide electricity at a variable price (as opposed to a fixed rate as in the traditional regulated framework). In addition, as integration gathers pace and affects fuel markets (such as coal or natural gas), input costs also become volatile. In a deregulated market, presumably only assets that enjoy a positive difference between the price of electricity and the price of a particular fuel used to generate it under prevailing market conditions will be operated. It is this spread that determines the economic value of a generation asset that can be used to transform the input fuel into output electricity. Thus, power operators pay close attention to the dark and spark spreads; Alberola et al. [2]. The dark spread represents the theoretical profit that a coal-fired power plant makes from selling a unit of electricity having purchased the fuel required to produce that unit of electricity. Similarly, the spark spread refers to the equivalent for natural gas-fired power plants. (This idea is analogous to the concept of the "crack spread" used in the oil/refining industry; Deng et al. [6]. It refers to the prices of crude oil and refined products like diesel or gasoline.)

On the other hand, within the EU Emissions Trading Scheme (ETS), the price of emission allowances can affect the cash flows of a power plant during its entire lifetime. Upon the introduction of carbon costs, the former spreads must be corrected by the allowance price. They become, respectively, the clean dark spread and the clean spark spread. As is well known, the option to switch from coal to natural gas in its inputs represents an abatement opportunity for a utility to reduce CO2 emissions in the short term. Therefore, the equilibrium between these spreads sets the carbon price above which it becomes profitable for an electricity producer to switch from coal to natural gas; Laurikka and Koljonen [14]. Conversely, as long as the carbon price remains below this switching price, coal plants are more profitable than gas plants, even after taking carbon costs into account. These indicators help to determine the preferred fuel used for power generation. Final consumers are also affected since allowance prices will presumably be passed on to electricity prices (either fully or in part).

This paper can be of interest also to U.S. utilities. In the EIA [8] reference case, coal-fired power plants continue to be the dominant source of electricity generation through 2030. Thus, coal share generation increases from 49% to 54%, and coal plants account for 40% of total capacity additions from 2006 to 2030. However, technology choices for new plants and utilization of existing capacity are affected by relative fuel costs and changes in environmental policies. Right now, there is no federal cap-and-trade mechanism to control CO_2 emissions. But a few multi-state or regional schemes are on the way, and federal legislation can eventually be established well before the next coal plants reach the end of their useful lives. If so, failure now to account properly for uncertain emission costs in investment decisions can press utilities into a rush for coal only to get their fingers burnt in the longer term. Indeed, many utilities are beginning to assess the potential cost of future carbon regulations within their resource plans. Following Barbose et al. [4], the mere prospect of that regulation is already having an impact on utilities' decision-making and resource choices.

Several papers address the valuation of electricity generating assets assuming separate dynamics for input and output prices. Hlouskova et al. [10] consider a coal-based electricity producing turbine in a liberalized market. They adopt a discrete-time model for the electricity spot price, which is a first-order autoregressive process with time-varying mean and a jump component. Coal price, instead, is assumed constant. Focusing on the relevant spot market for electricity in Germany, they value a typical electricity generating turbine alongside its optimal schedule. The (multi-stage) decision problem is solved by Monte Carlo simulation in conjunction with backward dynamic programming. Besides, the spot price model is used to simulate possible price paths for their sample period. The simulated profit-loss distribution represents the risk profile of the plant. This information can be used to integrate physical production assets with financial contracts for the purpose of enterprise-wide risk management.

Deng et al. [6] value both generation and transmission assets starting from futures contracts for electricity and the relevant fuel (e.g., natural gas). First they consider the case in which the futures price processes of electricity and gas for the relevant maturities follow geometric Brownian motions. Then they assume specific mean-reverting processes. Later on, Deng [5] extends the former model by adopting a more realistic electricity spot price model which explicitly takes into account jumps and spikes. Yet this process continues to be a onefactor model and as such has its drawbacks in matching the correlation structure of electricity forward prices with different maturities.

Laurikka [13] addresses the valuation of power technologies within an emissions trading scheme. He presents a simulation model in an operating environment with multiple exogenous and one-factor mean-reverting stochastic prices (among them, electricity, emission allowance, coal, natural gas). Laurikka and Koljonen [14] consider a similar environment; unlike the previous work, they consider two simple mean-reverting stochastic variables (the price of electricity and the emission allowance) and two deterministic variables (fuel price and the number of free allowances). Again, they adopt the Monte Carlo approach for plant valuation purposes.

Näsäkkälä and Fleten [15] follow a different approach. They take the viewpoint of an investor holding a license to build a gas-fired power plant. But they directly model the spark spread as a sum of short-term deviations (assumed to follow a simple mean-reverting process) and equilibrium price (assumed to follow a geometric Brownian motion). One advantage is that, as electricity and gas are often used for the same purposes (such as heating or cooling), their seasonal variations have similar phases and thus the seasonality decays from the spark spread. Also, it enables a more thorough and intuitive description of the investment decision process. As they point out, though, when using the spark spread process some information about its uncertainty structure may be lost compared to models with separate processes for input and output. However, after developing the two approaches, their results indicate that, with their data, the difference is small.

The purpose of this paper is to assess the risks in coal plants' earnings. Following a similar approach to Näsäkkälä and Fleten [15], we adopt the viewpoint of a utility which is operating a coal-fired power plant with a long useful life ahead (it is similar for an investor holding a license to build a coal-fired plant). Assuming it operates under the EU ETS, from the outset we naturally focus on the clean dark spread. Arguably, the prices of coal, natural gas, carbon and electricity are governed by stochastic processes. However, we do not propose separate dynamics for each of them. Somehow we blend the two approaches mentioned above. We start from the notion of the clean dark spread. But, instead of directly modelling it, we decompose it into three separate elements with simple interpretations. Then, we assume a specific continuous-time stochastic process for each of them.

First, we note that electricity price typically arises from supply and demand schedules. Thus, electricity is sold at the price requested by the marginal generating unit in the matching process. The cost of fuel composes most of the marginal cost of electricity. The structure of the merit order of suppliers may vary significantly from one country to another. Usually the marginal units are natural gas-fired plants; consequently the price of electricity is determined by the margin of this kind of technology, namely the clean spark spread (plus, possibly, other items as operating and maintenance costs, etc.). (Because gas-fired turbines produce relatively little pollution, and are quick and easy to start and ramp up, they are often the technology of choice for load following and peak generation; Douglas and Popova [7].) Yet the rest of the generating fleet in general, and coal-fired plants in particular, show a different pattern of fuel costs, emission costs, and the like. Under these circumstances, gas plants are better suited than coal plants to offset, at least partially, the risk in the cost side with the risk in the revenue side. Indeed, base load generators face their greatest risk of loss when prices and consumption fall, largely because they incur significant costs when they must shut down and restart base load power plants. Therefore their margins face a greater risk; note, though, that this does not necessarily mean less expected profits.

The first element in our decomposition of the clean dark spread is thus the clean spark spread. Similarly, the second one is also a composite item, namely the fuel price gap between coal and gas (per megawatt hour generated); the reason for doing so is explained below. But we do not further decompose these variables into other, more fundamental ones (e.g. the prices of electricity, gas, and so on); we directly model them as specific one-factor mean-reverting processes. As for the third element, the price of carbon dioxide, we assume it follows a standard geometric Brownian motion, and is treated as such in isolation. This may be a good compromise between information loss and intuitive explanation.

We estimate the three stochastic processes from actual market data. Thus we get numerical values of the underlying parameters. We then run a number of simulations for each of these three components. The whole time horizon comprises ten years, which span the Kyoto Protocol's commitment period (2008-12) and the next five-year period 2013-17. This time horizon is subdivided into many shorter time steps. At each step in a given simulation the resulting clean dark spread is derived; it is measured in euros per megawatt hour. Since this sum is received for one megawatt hour produced, income in that step equals the spread times the number of megawatts hour generated over that step. (The amount earned over any one time step may be interpreted as the sum that is contributed to the utility's income statement in that step.) Last, we just add up all the step contributions until the end of the time horizon considered. Thus we get an estimate of the cumulative income over the two five-year periods for a given simulation. Following this process a number of times allows us to assess not only the expected earnings but also the risk profiles. We note that there is no discounting in the valuation process since this is not deemed essential to the objective of the paper. According to our results, the earnings do remain positive over the commitment period. This no longer holds necessarily, though, in the immediate post-Kyoto period.

The remainder of our paper is organized as follows. In Section 2 we introduce some preliminaries about clean spreads along with the technical parameter values that will be used below. In Section 3 we explain the three stochastic processes that the aforementioned variables are assumed to follow. We describe our sample data and also the numerical estimates of the relevant parameters. In Section 4 we show the main results of our simulations regarding coal-based power plants under the EU ETS. Section 5 concludes.

2 Some preliminaries

2.1 Conceptual framework

Two different spreads can be defined. First, for a gas-fired plant the clean spark spread (CSS) is:

$$CSS = P_E - \frac{P_G}{E_G} - P_{CO_2}I_G,\tag{1}$$

where P_E denotes electricity price (\in/MWh), P_G is the price of natural gas (\in/MWh),¹ E_G is the net thermal efficiency of a gas-fired plant, and P_{CO_2} is the price of a EU emission allowance (\in/tCO_2). Last, I_G stands for the emission intensity of the plant (tCO_2/MWh); this in turn depends upon the net thermal efficiency of each gas-fired plant.

According to IPCC [11], a plant burning natural gas has an emissions factor of 56.1 $kgCO_2/GJ$.² Since under 100% efficiency conditions 3.6 GJ would be consumed per megawatt hour, we get:

$$I_G = \frac{0.20196}{E_G} \frac{tCO_2}{MWh}.$$
 (2)

Thus the complete formula for the CSS is:

$$CSS = P_E - \frac{1}{E_G} (P_G + 0.20196 \times P_{CO_2}).$$
(3)

Similarly, following IPCC [11] a plant burning bituminous coal has an emission factor of 94.6 $kgCO_2/GJ$ under 100% efficiency conditions; then:

$$I_C = \frac{0.34056}{E_C} \frac{tCO_2}{MWh}.$$
 (4)

Thus the complete formula for the Clean Dark Spread (CDS) is:

$$CDS = P_E - \frac{1}{E_C} (P_C + 0.34056 \times P_{CO_2}), \tag{5}$$

where P_C is the price of coal (\in/MWh) , and E_C denotes the net thermal efficiency of a coal-fired plant.

We can solve for P_E in Eq. (3) and then substitute into Eq. (5), thus linking the two spreads. This yields:

$$CDS = CSS + \frac{1}{E_G}(P_G + 0.20196 \times P_{CO_2}) - \frac{1}{E_C}(P_C + 0.34056 \times P_{CO_2}).$$
 (6)

Or, equivalently:

$$CDS = CSS + \left(\frac{P_G}{E_G} - \frac{P_C}{E_C}\right) + \left(\frac{0.20196 \times P_{CO_2}}{E_G} - \frac{0.34056 \times P_{CO_2}}{E_C}\right).$$
(7)

With regard to the right-hand side, the first term represents the margin derived by natural gas plants. The second one is the fuel price gap (adjusted for

 $^{^{1}1}$ MWh = 3.412 mmBTU, and 1 mmBTU = 0.293083 MWh.

 $^{^2 \, {\}rm This}$ corresponds to 15.311 kgC/GJ, since one ton of carbon is carried on 3.67 tons of $CO_2.$

relative efficiency rates). To the extent that this gap is positive, it is to the advantage of coal-fired plants. The last term, though, stands for the disadvantage of coal plants because of their higher carbon emissions, which is further aggravated by their lower efficiency levels.

Both spreads are equal CSS = CDS when:

$$\frac{P_G}{E_G} - \frac{P_C}{E_C} = \frac{0.34056 \times P_{CO_2}}{E_C} - \frac{0.20196 \times P_{CO_2}}{E_G},\tag{8}$$

i.e., when the advantage in fuel price is wiped out by the higher emission costs.

For high enough allowance prices, CDS can reach a low value or even become negative. Specifically, we would get CDS = 0 when:

$$CSS + \frac{P_G}{E_G} - \frac{P_C}{E_C} = \frac{0.34056 \times P_{CO_2}}{E_C} - \frac{0.20196 \times P_{CO_2}}{E_G},$$
(9)

i.e., when the higher costs of carbon permits offset not only the fuel price gap but the CSS as well.

Henceforth we adopt the typical case: $E_G = 0.55$ and $E_C = 0.40$. Then Eq. (2) implies overall emissions of $I_G = 0.3672 \ tCO_2/MWh$ from a gas plant; and Eq. (4) implies overall emissions of $I_C = 0.8514 \ tCO_2/MWh$ from a coal plant. In this case, CDS = 0 when:

$$CSS + \frac{P_G}{0.55} - \frac{P_C}{0.40} = \left(\frac{0.34056}{0.40} - \frac{0.20196}{0.55}\right) P_{CO_2} = 0.4842 P_{CO_2}.$$
 (10)

Hence, an increase of one euro in the allowance price reduces the CDS by 0.4842 \in /MWh .

2.2 Sample data

Our sample consists of four data sets: (1) daily electricity prices on PowerNext (France) from November 27th 2001 to February 6th 2008; (2) daily gas prices at Zeebrugge (Belgium) from April 4th 2001 to February 2nd 2008 as provided by Bloomberg; (3) daily spot carbon prices on the EU ETS from June 20th 2005 to January 28th 2008 as provided by BlueNext; (4) daily ARA coal one-month futures prices on the European Energy Exchange (Leipzig, Germany) from May 2nd 2006 to February 5th 2008. (In addition, prices of futures contracts on EU allowances from ICE have been used but only in Section 3.4 below, so we make no further reference to them here.) Sample prices come from markets that are geographically very close to each other. We focus on the time span over which the four price series are available, namely May-1-2006 to Jan-28-2008. We transform the daily series into weekly average prices. Thus, we have a complete data set over 92 weeks.

Figure 1 shows the time path of CSS and CDS series. Their main statistics appear in Table 1. The average CDS value is significantly higher than the mean CSS. To a large extent this is due to low CO_2 allowance prices; see Figure 2. Also, the advantage in fuel prices for a coal plant amounts to 8.8666 \in/MWh on average. We can get a crude estimate of the carbon price necessary to have CSS = CDS; a rough computation would lead to $\hat{P}_{CO_2} = \frac{8.8666}{0.4842} = 18.31 \in/tCO_2$. Similarly, Table 1 suggests that one would have CDS = 0 for $\tilde{P}_{CO_2} = \frac{11.281+8.8666}{0.4842} = 41.61 \in/tCO_2$. Below we propose and then estimate the stochastic processes that will allow us to set long-term equilibrium values and provide more exact estimates.

Table 1. Basic statistics of CSS and CDS weekly series.								
CSS	CDS	$\frac{P_G}{0.55} - \frac{P_C}{0.40}$						
11.281	19.766	8.8666						
8.2827	13.472	8.9994						
-17.338	-11.047	0.83517						
89.580	111.22	15.801						
15.717	18.839	4.0317						
1.3932	0.95312	0.45470						
2.4997	2.4814	-0.14031						
9.0810	7.6654	-1.0235						
	$\begin{array}{c} {\rm s~of~CSS~a}\\ \hline CSS\\ 11.281\\ 8.2827\\ -17.338\\ 89.580\\ 15.717\\ 1.3932\\ 2.4997\\ 9.0810\\ \end{array}$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $						

3 Stochastic models and econometric analysis

Following Eq. (6), first we assume specific continuous-time stochastic processes for each of the three items on the right-hand side. Then, we focus on their discrete-time counterparts. We estimate the coefficients on these regression equations with actual data from the markets involved. The relations between the coefficients in the discrete -time equations and the parameters in the continuoustime processes allow us to get numerical estimates of the latter from the former set of values. Subsequently we will use these parameter values in our MC simulations of the separate inputs to the CDS (and their sum).

3.1 The Clean Spark Spread

We adopt the simplest mean-reverting stochastic process (also known as an Ornstein-Uhlenbeck or O-U process):

$$dS_t = k_S (S_m - S_t) dt + \sigma_S dW_t^S, \tag{11}$$

where S_t denotes the value of the CSS at time t. This current value tends to the level of the CSS in the long term S_m at a speed of reversion k_s . Besides, σ_s is the instantaneous volatility of the CSS, and dW_t^s stands for the increment to a standard Wiener process.

This model allows CSS to take on negative and positive values. It is shown in Appendix A that S_t has a conditional mean

$$E(S_t) = S_0 e^{-k_S(t-t_0)} + S_m (1 - e^{-k_S(t-t_0)}),$$

which amounts to

$$E(S_{t+\Delta t}) = S_t e^{-k_S \Delta t} + S_m (1 - e^{-k_S \Delta t}).$$

Also, the conditional variance is

$$Var(S_t) = \frac{\sigma_S^2}{2k_S} [1 - e^{-2k_S(t-t_0)}].$$

Since both mean and variance remain finite as $t \to \infty$, this process is stationary.³

Eq. (11) is the continuous-time version of a first-order autoregressive process in discrete time:

$$S_{t+\Delta t} = S_m (1 - e^{-k_S \Delta t}) + S_t e^{-k_S \Delta t} + \varepsilon_{t+\Delta t}^S = a_S + b_S S_t + \varepsilon_{t+\Delta t}^S, \quad (12)$$

where $\varepsilon_t^S \sim N(0, \sigma_{\varepsilon}^S)$, and the following notation holds:

$$a_S \equiv S_m (1 - b_S) \Rightarrow S_m = \frac{a_S}{1 - b_S},$$
$$b_S \equiv e^{-k_S \Delta t} \Rightarrow k_S = -\frac{\ln b_S}{\Delta t}.$$

This process for the CSS is stationary if $b_S < 1$. Figure 3 shows the partial autocorrelation function of the CSS weekly series. Also, as shown in Appendix A:

$$\begin{split} (\sigma_{\varepsilon}^{S})^{2} &= \frac{\sigma_{S}^{2}}{2k_{S}}[1 - e^{-2k_{S}\Delta t}] \Rightarrow \\ \Rightarrow & \sigma_{S}^{2} = \frac{2k_{S}(\sigma_{\varepsilon}^{S})^{2}}{1 - e^{-2k_{S}\Delta t}} = \frac{2(\sigma_{\varepsilon}^{S})^{2}\ln b_{S}}{\Delta t[b_{S}^{2} - 1]}. \end{split}$$

The last three equations will allow us to recover the continuous-time process parameters (k_S, S_m, σ_S) upon estimation of the regression coefficients (a_S, b_S) and the standard deviation of the regression residuals (σ_{ε}^S) .

3.2 The adjusted price gap between coal and natural gas

Now we turn to the second term in Eq. (6)'s right hand. Figure 4 shows the prices of natural gas and coal along with the resulting gap between fuel prices (in \in/MWh produced) with the assumed efficiency rates. Again we adopt an Ornstein-Uhlenbeck process for the difference $P_G/0.55 - P_C/0.40$. We have another AR(1) process as its counterpart in discrete time:

$$C_{t+\Delta t} = C_m (1 - e^{-k_C \Delta t}) + C_t e^{-k_C \Delta t} + \varepsilon_{t+\Delta t}^C = a_C + b_C C_t + \varepsilon_{t+\Delta t}^C, \quad (13)$$

 $^{^{3}}$ The CSS can be traced back to several individual prices of inputs and outputs. It may be worth noting that Eq. (11) can be a good approximation of this spread even if the underlying prices themselves do not follow O-U processes (Sodal, Koekebakker, and Aadland [16]).

where C_t denotes the price gap at time t, C_m is the level of the gap in the long term, and k_C stands for the speed of reversion. The remainder of the notation goes as before.

3.3Joint estimation of CSS and fuel price gap

It is possible that both the CSS series and the price gap series are affected by common factors. This possibility suggests that separate estimation of each equation may not be suitable. Instead, we estimate them as a first-order vector autoregressive (VAR) process:

$$S_{t+\Delta t} = a_S + b_S S_t + \varepsilon_{t+\Delta t}^S, \tag{14}$$

$$C_{t+\Delta t} = a_C + b_C C_t + \varepsilon_{t+\Delta t}^C. \tag{15}$$

The VAR(1) estimates of the coefficients in Eqs. (14) and (15) appear in the left hand of Table 2; they are statistically significant. From the series of residuals in both regressions we compute a correlation coefficient $\rho_{S,C} = 0.2538$. The right hand of Table 2 shows the values of the underlying parameters in the stochastic processes ($\Delta t = 1/52$, weekly observations) implied by these estimates.

Table 2. Estimates of the CSS and fuel price gap series.									
Coefficient	Coefficient Estimate t-statistic Parameter								
$\widehat{a_S}$	5.7196	3.400	k_S	34.0747					
$\widehat{b_S}$	0.5202	6.071	S_m	11.9216					
$\widehat{a_C}$	1.3285	2.629	σ_S	127.65					
$\widehat{b_C}$	0.8494	16.374	k_C	8.5068					
σ^S_{ε}	13.2060		C_m	8.8256					
σ_{ε}^{C}	2.0458		σ_C	15.9928					

A low value of $\widehat{b_S}$ implies that the process for CSS quickly reverts back to its long-term mean, as can be seen in the high value of k_s . Figure 5 displays both the observed CSS values and those predicted by the model. Instead, b_C is closer to one, which means that the fuel price gap behaves more like a random walk, as shown by a lower speed of reversion k_C .

Threshold allowance price for CDS = CSS and CDS = 0. Using the

parameter values of S_m and C_m in a deterministic context yields: a) CDS = CSS for a carbon price $\hat{P}_{CO_2} = \frac{C_m}{0.4842} = 18.23 \notin /tCO_2$. Below this level, CDS > CSS would hold and coal-based technology would be preferred.

b) CDS = 0 for a carbon price $\tilde{P}_{CO_2} = \frac{C_m + S_m}{0.4842} = 42.85 \notin /tCO_2$. Above this level, CDS < 0 would hold and coal-fired plants would be shunned.

The results of the above analysis broadly agree with the empirical evidence in Table 1. There, the implied values were $18.31 \in /tCO_2$ and $41.61 \in /tCO_2$, respectively.

Thus, if electricity price is set by gas-fired plants, a sizeable rise in the allowance price would be enough to offset the initial advantage in fuel price enjoyed by coal-fired plants. These stations could even cease to be profitable in the absence of carbon-capture units.

3.4 Stochastic process for the emission allowance price

During the Kyoto Protocol's commitment period (2008-2012) we assume that carbon price A_t (in \in/tCO_2) follows a geometric Brownian motion (GBM):

$$dA_t = \alpha A_t dt + \sigma_A A_t dW_t^A. \tag{16}$$

Therefore, the expected value for the allowance price in the near future is:

$$E(A_t) = A_0 e^{\alpha t} \quad \text{for } t < 5. \tag{17}$$

At the end of this period we assume there will be a sudden jump J in price, which would push the expected value upwards:

$$t = 5^{-}: E(A_t) = A_0 e^{5\alpha},$$

$$t = 5^{+}: E(A_t) = A_0 e^{5\alpha} + J.$$

From then on, we assume allowance scarcity is just right as an environmental policy measure and price evolves once again following a GBM:

$$E(A_t) = A_0 e^{\alpha t} + J e^{\alpha (t-5)} \text{ for } t > 5.$$
(18)

No further jumps are assumed in subsequent years for the sake of simplicity. Though environmental policy is conceivably expected to become stricter and push allowance prices to new heights at the end of this period, it is hard to foresee what will happen then.⁴

Estimation. The European Climate Exchange (ECX) manages the European Climate Exchange Financial Instruments (ECX CFI), which are traded at the London-based International Petroleum Exchange (later acquired by the Intercontinental Exchange, or ICE). Futures prices from ICE have been used here.

As this paper was developed, there were futures contracts for both the threeyear trial trading period (2005-2007) and the commitment period (2008-2012). Our sample starts on May 1st 2006 and closes on March 26th 2008. We thus have 495 daily prices for each of the five futures contracts maturing from Dec-08 to Dec-12.

⁴In January 2008 the European Commission presented a proposal to revise and strengthen the ETS. Some of the main changes are the following: (a) There will be one EU-wide cap on the number of emission allowances instead of 27 national caps. The annual cap will decrease along a linear trend line, which will continue beyond the end of the third trading period (2013-2020). (b) A much larger share of allowances will be auctioned instead of allocated free of charge. (c) Harmonised rules governing free allocation will be introduced.

Parameter estimation for the commitment period is developed as follows. First, we focus on the days for which observed futures prices are available. Then we estimate the spot price on each day by means of cubic splines that pass along the observed quotes on those days; see Figure 6 for a particular day. This procedure is briefly described in Appendix B. Estimation results of the spot price and nearby futures prices are plotted in Figure 7.

According to Ito's Lemma, the transformed variable $X_t \equiv \ln A_t$ follows a stochastic process:

$$dX_t = \left(\alpha - \frac{\sigma_A^2}{2}\right)dt + \sigma_A dW_t^A.$$
(19)

Hence, in discrete time:

$$y_t = \Delta \ln A_t = \ln A_t - \ln A_{t-\Delta t} = \left(\alpha - \frac{\sigma_A^2}{2}\right) \Delta t + \sigma_A \sqrt{\Delta t} \epsilon_t^3, \qquad (20)$$

where ϵ_t^3 is a standard Gaussian white noise.

We carry out our estimation according to the maximum likelihood (ML) method:

$$\arg\min_{\alpha,\sigma_A} \sum_{t=1}^{T} \left[-\frac{1}{2}\ln(\frac{\sigma_A^2}{\Delta t}) - \frac{1}{2}\frac{(y_t - (\alpha - \frac{\sigma_A^2}{2})\Delta t)^2}{\sigma_A^2 \Delta t}\right].$$

This method (conditioned on the first observation A_0) provides the estimators of the mean and variance of y_t . They are given by:

$$\widehat{m} = \frac{1}{T} \sum_{t=1}^{T} y_t, \quad \widehat{s}^2 = \frac{1}{T} \sum_{t=1}^{T} (y_t - \widehat{m})^2.$$
(21)

On this occasion, we use the whole series of (almost five hundred) daily returns. These equations yield: $\hat{m} = 0.00051248$, $\hat{s}^2 = 0.00082893$.

The ML estimators of the drift $(\hat{\alpha})$ and volatility $(\hat{\sigma}_A)$ parameters are derived from their relations to the mean and variance parameters. Note that both \hat{m} and \hat{s}^2 are expressed in daily terms, whereas $\hat{\alpha}$ and $\hat{\sigma}_A^2$ are customarily expressed in yearly terms. We take the number of trading days over a year to be 250. Therefore we have $\Delta t = 1/250$, and ML estimation yields: $\hat{\sigma}_A^2 = \hat{s}^2/\Delta t = 250\hat{s}^2 = 0.2072$. Hence we get a volatility estimate of $\hat{\sigma}_A = 0.4552$. In this respect, if instead we adopt moving windows of 50 observations, volatility estimates evolve as shown in Figure 8. A value (here assumed constant) of 0.4552 does not seem off the mark.⁵

Regarding the estimation of the drift, this would be:

$$\widehat{\alpha} = \frac{\widehat{m}}{\Delta t} + \frac{\widehat{s}^2}{2\Delta t} = 250\widehat{m} + 125\widehat{s}^2 = 0.2317.$$

 $^{^5}$ Also, Abadie and Chamorro [1] estimate σ_A from a similar sample by applying the Kalman filter. The numerical value is 0.4683.

Thus, the drift parameter of the process for X_t is: $\hat{\alpha} - \hat{\sigma}_A^2/2 = 250\hat{m} = 0.1281$. According to Gourieroux and Jasiak [9], asymptotic variances are given by:

$$V_{asy}(\hat{\sigma}_A^2) = \frac{2\sigma_A^4}{T} = 0.00017529, \quad V_{asy}(\hat{\alpha}) = \frac{\sigma_A^2}{T\Delta t} + \frac{\sigma_A^4}{2T} = 0.10577.$$

While volatility can be estimated accurately, this does not hold for the drift. Its asymptotic variance converges only mildly as the number of observations increases because of the term $T\Delta t$ which, in our case, amounts to 490/250 = 1.96; this is why it has fallen only to half $\hat{\sigma}_A^2$. Consequently, in what follows we use the volatility estimate but not that of the drift; instead, we adopt a range of possible values $\alpha = \{-0.025, 0.00, 0.025, 0.05, 0.075, 0.10\}$ and analyze their effect.

Last, residuals from regression Eqs. (14), (15), and (20) allow us to compute the correlation coefficients: $\rho_{S,A} = -0.0122$, $\rho_{C,A} = 0.0994$.

4 Monte Carlo simulation

As stated earlier, our aim is to study value and risk involved in coal stations operating under the EU ETS after Kyoto Protocol's expiration. We accomplish this by means of simulation techniques.⁶

4.1 The components of the CDS in isolation

Correlated random variables are generated according to the scheme (see Appendix C):

$$S_{t+\Delta t} = S_m (1 - e^{-k_S \Delta t}) + S_t e^{-k_S \Delta t} + \sigma_S \sqrt{\frac{1 - e^{-2k_S \Delta t}}{2k_S}} \epsilon_t^1, \qquad (22)$$

$$C_{t+\Delta t} = C_m (1 - e^{-k_C \Delta t}) + C_t e^{-k_C \Delta t} + \sigma_C \sqrt{\frac{1 - e^{-2k_C \Delta t}}{2k_C}} [\epsilon_t^1 \rho_{S,C} + \epsilon_t^2 \sqrt{1 - \rho_{S,C}^2}],$$
(23)

$$\ln A_{t+\Delta t} = \ln A_t + (\alpha - \frac{\sigma_A^2}{2})\Delta t + \sigma_A \sqrt{\Delta t} [\epsilon_t^1 \rho_{S,A} + \epsilon_t^2 \frac{\rho_{C,A} - \rho_{S,A} \rho_{S,C}}{\sqrt{1 - \rho_{S,C}^2}} + \epsilon_t^3 \sqrt{1 - \rho_{S,A}^2 - \frac{(\rho_{C,A} - \rho_{S,A} \rho_{S,C})^2}{1 - \rho_{S,C}^2}}],$$

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 $^{^{6}\}mathrm{Alesii}$ [3] develops a similar approach and shows a numerical example in the context of shipping finance.

$$A_{t+\Delta t} = A_t e^{(\alpha - \frac{\sigma_A^2}{2})\Delta t + \sigma_A} \sqrt{\Delta t [\epsilon_t^1 \rho_{S,A} + \epsilon_t^2 \frac{\rho_{C,A} - \rho_{S,A} \rho_{S,C}}{\sqrt{1 - \rho_{S,C}^2}} + \epsilon_t^3 \sqrt{1 - \rho_{S,A}^2 - \frac{(\rho_{C,A} - \rho_{S,A} \rho_{S,C})^2}{1 - \rho_{S,C}^2}}$$
(24)

where ϵ_t^1 , ϵ_t^2 and ϵ_t^3 are standardized Gaussian white noises with zero correlation. The first expression above is derived after replacing σ_{ε}^S in terms of σ_S . Similarly in the second expression. At the same time, if samples from a standardized bivariate normal distribution are required, an appropriate procedure is the one shown above, where $\rho_{S,C}$, $\rho_{S,A}$ and $\rho_{C,A}$ are the correlation coefficients between the variables in the multivariate distribution.

In order to get numerical estimates 40,000 sample paths for S_t , C_t and A_t are generated. Each path comprises 600 steps; this means five steps per month since the horizon considered is ten years, namely the five-year commitment period plus the next five years.

Starting values appear in Table 3; they have been computed above. As initial values of the CSS and the gap in fuel prices (in \in/MWh) we adopt the long-term equilibrium values. The initial allowance price is the one estimated on 03/26/2008, the last day of the sample used to estimate this market's parameters.

Table 3. Initial parameter values of the MC simulation.							
CSS	$S_0 = S_m = 11.9216$	$k_S = 34.0747$	$\sigma_S = 127.65$				
Fuel price gap	$C_0 = C_m = 8.8256$	$k_C = 8.5068$	$\sigma_C = 15.9928$				
Allowance price	$A_0 = 22.0923$	_	$\sigma_A = 0.4552$				
Correlation	$\rho_{S,C}=0.2538$	$\rho_{S,A} = -0.0122$	$\rho_{C,A}=0.0994$				

Computations are realized per unit of installed capacity (MW) and assume that the coal-fired plant operates 80% of the time on average (i.e. $8,760 \times 0.8 =$ 7,008 hours over a year). (For any other percentage rate, computations would vary proportionately for each *MW* of installed capacity.) Hence we assume a yearly production of 7,008 *MWh* for each megawatt installed. Since 60 time steps are used per year, this implies that 116.8 *MWh* will be generated per step for each MW of capacity.

At the final time t = 10, the distributions of the CSS and the fuel price gap are characterized by the statistics in Table 4. The theoretical mean for t = 10amounts to the long-term level estimated before. The theoretical volatility for t = 10 is computed according to the following formulas (see Appendix A):

$$\sigma_{S,t=10} = \sigma_S \sqrt{\frac{1 - e^{-20k_S}}{2k_S}} = 15.4629, \quad \sigma_{C,t=10} = \sigma_C \sqrt{\frac{1 - e^{-20k_C}}{2k_C}} = 3.8066$$

ſ	Table 4.	Statistics	of t	theoretical	and	simulated	CSS	and	fuel	price gap.
										O

	CS	S	Fuel price gap		
	Theoretical Simulated		Theoretical	Simulated	
Mean	11.9216	11.8502	8.8256	8.8525	
Volatility	15.4629	15.3780	3.8066	3.8673	

As for the allowance price, the final distribution at time t = 10 of the allowance prices depends on the growth rate α used and the jump that would take place at the end of the commitment period. For example, in the case of $\alpha = 0.05$ and a jump of 2.5 euros, the theoretical value of the mean would be:

$$E(A_{t=10}) = A_o e^{0.50} + 2.5 e^{0.25} = 39.6341,$$

as opposed to the mean from the 40,000 simulations of $40.143 \in /tCO_2$.

On the other hand, when $\alpha = 0.05$ and the jump size is $0.0 \in$, the theoretical value of volatility would be:

$$\sigma_{A,t=10} = \sigma_A \sqrt{10} = 1.4395.$$

This figure is very close to the value of 1.4409 derived from computing the standard deviation of the (natural log) prices of the emission allowance at the end of the MC simulation. These similarities attest to the goodness of our sample paths.

4.2 The overall CDS

Tables 5-7 below show our results under different scenarios. We focus on average earnings as derived from CDS values in Table 5 along with the 5% and 10% percentiles in Tables 6 and 7. (We disregard other inputs to the plant's net final profit.)

As already mentioned, the ten-year horizon is partitioned into 600 time steps, or 60 steps per year. Also, we are assuming a yearly production of 7,008 MWh for each megawatt of capacity installed; thus 116.8 MWh are generated over each step. The contribution of one step to the utility's economic results emanates from this output electricity and the accompanying CDS over this step. Aggregating over the first 300 time steps we compute the cumulative contribution of the plant to the firm's profits during the Kyoto period 2008-2012; similarly for the last 300 steps and the post-Kyoto period 2013-2017. No discounting is involved to better resemble what would show up in the utility's internal financial statements.

Look, for instance, at the Kyoto period under the assumption $\alpha = 0.0\%$ (first row in Table 5). When emission allowances are not expected to appreciate, the plant earns 352,000 euros over that time horizon (for megawatt installed). The output generated over this five-year period amounts to 7,008 × 5 = 35,040 *MWh*. Therefore the firm would get on average some $10.05 \notin /MWh$.⁷ Next period (2013-17), if the expected drift rate remains at zero and there is no jump in allowance price, the average CDS remains almost the same, namely 348,000 euros (see next line in Table 5). (These values are not exactly equal since random samples are being generated in both cases and average values

⁷This is much lower than the average CDS of 19.76 that appears in Table 1. This is partly due to low allowance prices during that sample period (Figure 2). According to our analysis, this is not what carbon market seems to suggest for the near future.

Table 5. Expected earnings per megawatt installed (thousand \in)									
	$\alpha = -2.5\%$	$\alpha = 0$	$\alpha = 2.5\%$	$\alpha = 5\%$	$\alpha=7.5\%$	$\alpha = 10\%$			
2008-12	374	352	327	300	271	239			
2013-17									
$J = 0.0 \in$	413	348	270	174	58	-84			
$J = 2.5 \in$	373	306	224	126	6	-140			
$J = 5.0 \in$	333	263	179	78	-45	-194			
J = 7.5 €	293	221	134	29	-97	-249			
$J = 10 \in$	253	178	89	-19	-148	-304			

may diverge slightly.) Obviously, if carbon price jumps upwards the CDS falls accordingly; similarly for changes in the value of the drift rate, α .

Table 6. Earnings 10% percentile (thousand \in) in 2013-17.									
	$\alpha = -2.5\%$	$\alpha = 0$	$\alpha=2.5\%$	$\alpha = 5\%$	$\alpha=7.5\%$	$\alpha = 10\%$			
$\mathbf{J}=0.0 \Subset$	17	-126	-300	-511	-770	-1,091			
$J=2.5 \Subset$	-41	-187	-365	-583	-847	-1,166			
$J=5.0 \Subset$	-98	-249	-431	-652	-922	-1,247			
$J=7.5 \in$	-156	-310	-496	-723	-996	-1,328			
$\mathbf{J}=10 \Subset$	-216	-374	-564	-797	-1,077	-1,409			

Table 7. Earnings 5% percentile (thousand \in) in 2013-17.									
	$\alpha = -2.5\%$	$\alpha = 0$	$\alpha=2.5\%$	$\alpha = 5\%$	$\alpha=7.5\%$	$\alpha = 10\%$			
$J = 0.0 \in$	-357	-586	-854	-1,187	-1,596	-2,096			
$J = 2.5 \in$	-423	-652	-930	-1,271	$-1,\!685$	-2,191			
$\mathbf{J}=5.0 \Subset$	-494	-727	-1,011	-1,355	-1,776	-2,290			
$\mathbf{J}=7.5 \Subset$	-562	-800	-1,093	-1,443	-1,871	-2,386			
$J = 10 \in$	-634	-880	-1,176	-1,534	-1,965	-2,492			

It can be seen in Table 5 that, over the commitment period (2008-12), the expected average CDS takes on a positive value. Nonetheless, for values of the drift parameter $\alpha \geq 5\%$, the expected CDS may turn to negative in the period 2013-17, the more so depending on the potential jump in allowance prices during the transition from one period to the next. These results are displayed in Figure 9.

Tables 6 and 7 show the Earnings at Risk (EaR) of coal-fired plants in the 2013-17 phase. According to Table 6, in the absence of a jump and for $\alpha = 5.0\%$, there is a 10% of potential states in which losses would surpass 511,000 euros for each megawatt of capacity installed if electricity is produced under such circumstances. As shown in Table 7, in the same scenario $(J = 0.0 \\ \in \\$ and $\alpha = 5.0\%$), the losses would go beyond 1 million euros in the worst 5% of situations. See Figure 10. Presumably a coal-fired plant would not operate under such circumstances, unless other reasons imply so (signed guarantees or the like). (Nonetheless the figures may be taken as such so as to maintain the level basis for comparisons.)

5 CONCLUSIONS

Present and future liabilities by EU utilities in relation to CO2 emissions create a setup previously unknown. Current legislation entails new costs and risks to the generating firms. Fortunately they are getting better gauged as markets develop and price series get longer.

We assume that electricity fetches a market price which is determined by natural gas combined-cycle plants operating as the marginal generating units. We further assume that the price gap between gas and coal follows a meanreverting process. Even though coal-fired plants enjoy an initial advantage in terms of cheap fuel for generating electricity, an increase in the price of the emission allowances may erode significantly their profit margins. Given that the future path of the allowances is hard to forecast (specially after 2012), we have designed potential scenarios depending on the drift rate of the allowance price and the jump size of the price at the end of the commitment period. Under these assumptions we have assessed the risks on the profit margins of coal plants.

Margins do remain positive over the Kyoto Protocol's commitment period. This no longer holds necessarily, though, in the immediate five years after the Protocol's expiration. Expected margins may switch to negative, or remain slightly positive but with a high risk of becoming negative in many cases. In such scenarios, this would lead to shut down the coal plant thus reducing the chances to recover the investment costs.

Realization of scenarios involving steep growth in the allowance price would be incompatible with investing in new coal plants. It could even trigger the abandonment of plants currently in operation but with relatively short useful lives as carbon prices climb ever higher. However, the decision to abandon a power plant may be affected by provisions in the National Allocation Plants concerning assigned allowances in the case of plant closures. Also, a high allowance price could be compatible with coal-based electricity generation if there are gains in efficiency rates and the plants are retrofitted with carbon capture and storage units, for example.

Similarly, in the case of developing countries still unaffected by the Kyoto Protocol, the signing and ensuing adaptation may put current investments in this technology at risk. Consequently, the decision to undertake new investments should take this possibility into account.

A Moments of a mean-reverting O-U process

We start from the stochastic model:

$$dS_t = k(S_m - S_t)dt + \sigma_t dW_t$$

Next we adopt the notation in Kloeden and Platen [12]. The homogeneous equation is:

$$\frac{dS_t}{S_t} = -kdt$$

Therefore, its fundamental solution is $\Phi_{t,t_0} = e^{-k(t-t_0)}$ and making $Y_t = \Phi_{t,t_0}^{-1}S_t = e^{k(t-t_0)}S_t$ derivatives can be computed:

$$\frac{dY_t}{dS_t} = e^{k(t-t_0)}; \ \frac{d^2Y_t}{dS_t^2} = 0; \ \frac{dY_t}{dt} = ke^{k(t-t_0)}S_t.$$

By Ito's Lemma:

$$dY_t = d(\Phi_{t,t_0}^{-1}S_t) = kS_m e^{k(t-t_0)} dt + e^{k(t-t_0)} \sigma_t dW_t$$

hence we deduce that:

$$S_t = S_0 e^{-k(t-t_0)} + e^{-k(t-t_0)} k \int_{t_0}^t e^{k(s-t_0)} ds + e^{-k(t-t_0)} \sigma \int_{t_0}^t e^{k(s-t_0)} dW_s.$$

The first moment can be easily reached:

$$E(S_t) = S_0 e^{-k(t-t_0)} + S_m (1 - e^{-k(t-t_0)});$$

therefore:

$$E(S_{\infty}) = S_m$$

The variance is given by:

$$Var(S_t) = e^{-2k(t-t_0)}\sigma^2 \int_{t_0}^t e^{2k(s-t_0)} ds = \frac{\sigma^2}{2k} [1 - e^{-2k(t-t_0)}].$$

B Estimation of the cubic spline

Each day we need to trace a curve that passes through all the points in the price/time space for which futures prices are available. For this purpose we use four pieces of curves of the form:

$$y_t = a_{08}t^3 + b_{08}t^2 + c_{08}t + d_{08} \text{ for } t_{08} \leq t \leq t_{09},$$

$$y_t = a_{09}t^3 + b_{09}t^2 + c_{09}t + d_{09} \text{ for } t_{09} \leq t \leq t_{10},$$

$$y_t = a_{10}t^3 + b_{10}t^2 + c_{10}t + d_{10} \text{ for } t_{10} \leq t \leq t_{11},$$

$$y_t = a_{11}t^3 + b_{11}t^2 + c_{11}t + d_{11} \text{ for } t_{11} \leq t \leq t_{12},$$

where t_{08} , t_{09} , t_{10} , t_{11} and t_{12} denote the time of maturity of the futures contracts from December-08 to December-12. For the sake of simplicity, and without loss of generality, we take $t_{08} = 0$; then $t_{09} = 1$, $t_{10} = 2$, $t_{11} = 3$ and $t_{12} = 4$.

Since there are 16 parameters to estimate we need the same number of restrictions to get a unique solution:

a) The pieces of the cubic functions must reach the points actually observed; this provides eight equations.

b) The first derivatives in t_{09}, t_{10} and t_{11} must coincide; three equations.

c) Coincidence of the second derivatives in t_{09}, t_{10} and t_{11} ; three equations.

d) The last two conditions have been chosen so as to get a natural spline; this requires that second derivatives at the initial and final points take on a value of zero.

The first cubic on each day, substituting the time to maturity of the Dec-08 futures contract with negative sign, allows to get an estimate for the spot price of the emission allowance on that day A_0 . This can be seen in Figure 6.

C Generation of mean-reverting correlated variables

Let e_1 , e_2 , and e_3 be standard normal deviates. Random samples of correlated variables can be generated as follows:

$$x_1 = f_{11}e_1,$$
 (26)

$$x_2 = f_{21}e_1 + f_{22}e_2, (27)$$

$$x_3 = f_{31}e_1 + f_{32}e_2 + f_{33}e_3, (28)$$

if $Cov(x_1, x_2) = \rho_{12}$, $Cov(x_1, x_3) = \rho_{13}$, and $Cov(x_2, x_3) = \rho_{23}$.

Random deviates with this correlation structure must satisfy:

$$\begin{split} E(x_1^2) &= 1 \Longrightarrow f_{11} = 1, \\ E(x_1x_2) &= \rho_{12} \Longrightarrow f_{21} = \rho_{12}, \\ E(x_2^2) &= 1 = f_{21}^2 + f_{22}^2 \Longrightarrow f_{22} = \sqrt{1 - \rho_{12}^2}, \\ E(x_1x_3) &= \rho_{13} = f_{11}f_{31} \Longrightarrow f_{31} = \rho_{13}, \\ E(x_2x_3) &= \rho_{23} = f_{21}f_{31} + f_{22}f_{32} \Longrightarrow f_{32} = \frac{\rho_{23} - \rho_{12}\rho_{13}}{\sqrt{1 - \rho_{12}^2}}, \\ E(x_3^2) &= 1 = f_{31}^2 + f_{32}^2 + f_{33}^2 = \rho_{13}^2 + \frac{(\rho_{23} - \rho_{12}\rho_{13})^2}{1 - \rho_{12}^2} + f_{33}^2 \Longrightarrow f_{33} = \sqrt{1 - \rho_{13}^2 - \frac{(\rho_{23} - \rho_{12}\rho_{13})^2}{1 - \rho_{12}^2}}. \end{split}$$

Henceforth:

$$x_1 = e_1, (29)$$

$$x_2 = e_1 \rho_{12} + e_2 \sqrt{1 - \rho_{12}^2}, \tag{30}$$

$$x_3 = e_1\rho_{13} + e_2\frac{\rho_{23} - \rho_{12}\rho_{13}}{\sqrt{1 - \rho_{12}^2}} + e_3\sqrt{1 - \rho_{13}^2 - \frac{(\rho_{23} - \rho_{12}\rho_{13})^2}{1 - \rho_{12}^2}}.$$
 (31)

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Figure 1: Clean dark spread and clean spark spread, May-2006 to Jan-2008.



Figure 2: Carbon price (\in /MWh) for gas- and coal-based technologies (assuming net thermal efficiencies $E_G = 55\%$ and $E_C = 40\%$).

Partial Autocorrelation Function



Figure 3: Partial autocorrelation function of the CSS series.



Figure 4: Natural gas (Zeebrugge) price, coal ARA price, and fuel price gap.



Real and Estimated CSS

Figure 5: Actual and estimated CSS series.



Figure 6: Spline-based estimation of spot price from futures prices (March 26th 2008).

Spot Cubic Spline Estimation



Figure 7: Spot estimates and nearby futures prices.



50-day moving window Volatility of Spot Estimated Allowances Prices

Figure 8: Volatility of spot allowance price over 50-days moving windows.



Figure 9: Expected earnings in the Kyoto period (2008–12) and beyond (2013-17).



Figure 10: Earnings at Risk beyond Kyoto (2013-17): 5% and 10% percentiles.